

**coefficient of determination ( $r^2$ )**

A normalized measure of discrepancy that expresses the fraction of *variance* that is explained by a statistical *model* (“explained variance”). The coefficient is usually denoted by the symbol  $r^2$ . Its value is in the interval  $[0, 1]$ . A large fraction of explained variance indicates a good fit of the model to the data. The coefficient of determination is calculated as follows:

$$r^2 = \frac{TSS - RSS}{TSS} = 1 - \frac{RSS}{TSS} = 1 - \frac{\sum(y - f(x))^2}{\sum(y - \bar{y})^2}$$

where  $y$  is an actual outcome,  $\bar{y}$  is the mean of outcomes, and  $f(x)$  is a prediction based on an *independent variable*  $x$  made by the model  $f$ . The *residual sum of squares* (RSS) measures the unexplained variance and the *total sum of squares* (TSS) the total variance. Their difference is the explained variance. See figure COD. See also: *linear regression*.

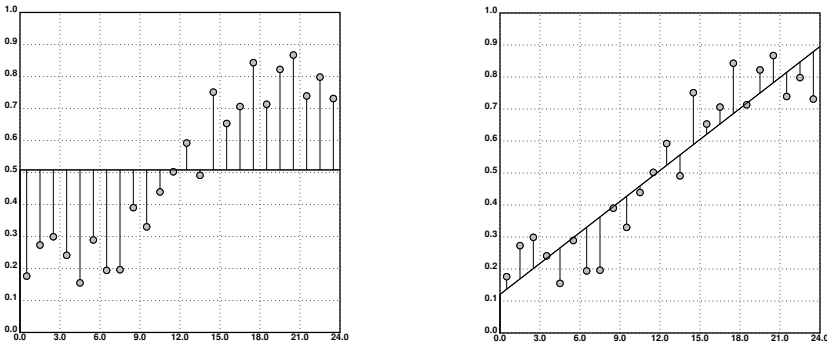


Figure **COD**: left: total variance (TSS); right unexplained variance (RSS) given a linear model; their difference is the explained variance (TSS–RSS) of the model