

**correlation coefficient** (Pearson's  $r$ ,  $r$ ,  $\rho$ )

A normalized measure indicating the degree of *correlation* between two *random variables*  $X$  and  $Y$ , where  $r \approx 0$  means that the variables are asymptotically uncorrelated,  $r = 1$  indicates perfect correlation ( $X = Y$ ) and  $r = -1$  indicates perfect anticorrelation ( $X = -Y$ ). The correlation coefficient is defined as:

$$\rho_{X,Y} = \frac{\text{cov}(X,Y)}{\sigma_X \sigma_Y}$$

where  $\text{cov}(X, Y)$  is the *covariance* of  $X$  and  $Y$  and  $\sigma_X$  and  $\sigma_Y$  are the *standard deviations* of  $X$  and  $Y$ , respectively.

A similar operator exists for *samples* but, since no *Bessel's correction* is needed ( $\rightarrow$  *covariance*), it is in fact equal to the above. Formally, it is defined as:

$$r_{x,y} = \frac{s_{x,y}}{s_x s_y}$$